

## JEE (ADVANCED) 2019 PAPER 2

### PART-I PHYSICS

#### SECTION 1 (Maximum Marks: 32)

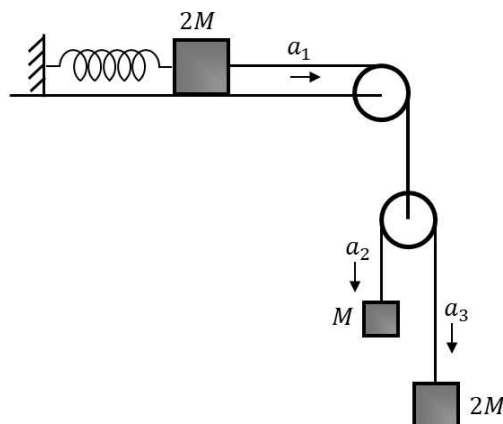
- This section contains EIGHT (08) questions.
- Each question has FOUR options. ONE OR MORE THAN ONE of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:
 

Full Marks	: +4	If only (all) the correct option(s) is(are) chosen;
Partial Marks	: +3	If all the four options are correct but ONLY three options are chosen;
Partial Marks	: +2	If three or more options are correct but ONLY two options are chosen and both of which are correct;
Partial Marks	: +1	If two or more options are correct but ONLY one option is chosen and it is a correct option;
Zero Marks	: 0	If none of the options is chosen (i.e. the question is unanswered);
Negative Marks	: -1	In all other cases.
- For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then
  - choosing ONLY (A), (B) and (D) will get +4 marks;
  - choosing ONLY (A) and (B) will get +2 marks;
  - choosing ONLY (A) and (D) will get +2 marks;
  - choosing ONLY (B) and (D) will get +2 marks;
  - choosing ONLY (A) will get +1 mark;
  - choosing ONLY (B) will get +1 mark;
  - choosing ONLY (D) will get +1 mark;
  - choosing no option (i.e. the question is unanswered) will get 0 marks; and
  - choosing any other combination of options will get -1 mark.

- Q.1 A thin and uniform rod of mass  $M$  and length  $L$  is held vertical on a floor with large friction. The rod is released from rest so that it falls by rotating about its contact-point with the floor without slipping. Which of the following statement(s) is/are correct, when the rod makes an angle  $60^\circ$  with vertical?  
 [ $g$  is the acceleration due to gravity]

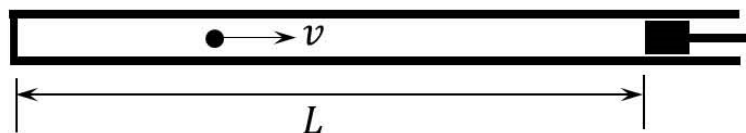
- (A) The angular speed of the rod will be  $\sqrt{\frac{3g}{2L}}$
- (B) The angular acceleration of the rod will be  $\frac{2g}{L}$
- (C) The radial acceleration of the rod's center of mass will be  $\frac{3g}{4}$
- (D) The normal reaction force from the floor on the rod will be  $\frac{Mg}{16}$

- Q.2 A block of mass  $2M$  is attached to a massless spring with spring-constant  $k$ . This block is connected to two other blocks of masses  $M$  and  $2M$  using two massless pulleys and strings. The accelerations of the blocks are  $a_1, a_2$  and  $a_3$  as shown in the figure. The system is released from rest with the spring in its unstretched state. The maximum extension of the spring is  $x_0$ . Which of the following option(s) is/are correct? [ $g$  is the acceleration due to gravity. Neglect friction]



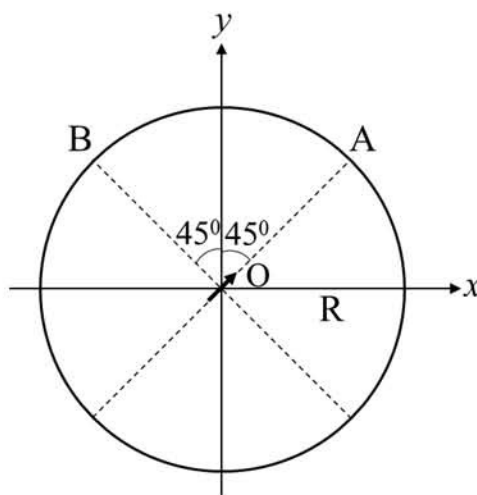
- (A)  $x_0 = \frac{4Mg}{k}$
- (B) When spring achieves an extension of  $\frac{x_0}{2}$  for the first time, the speed of the block connected to the spring is  $3g\sqrt{\frac{M}{5k}}$
- (C) At an extension of  $\frac{x_0}{4}$  of the spring, the magnitude of acceleration of the block connected to the spring is  $\frac{3g}{10}$
- (D)  $a_2 - a_1 = a_1 - a_3$

- Q.3 A small particle of mass  $m$  moving inside a heavy, hollow and straight tube along the tube axis undergoes elastic collision at two ends. The tube has no friction and it is closed at one end by a flat surface while the other end is fitted with a heavy movable flat piston as shown in figure. When the distance of the piston from closed end is  $L = L_0$  the particle speed is  $v = v_0$ . The piston is moved inward at a very low speed  $V$  such that  $V \ll \frac{dL}{L} v_0$ , where  $dL$  is the infinitesimal displacement of the piston. Which of the following statement(s) is/are correct?



- (A) The rate at which the particle strikes the piston is  $v/L$
- (B) After each collision with the piston, the particle speed increases by  $2V$
- (C) If the piston moves inward by  $dL$ , the particle speed increases by  $2v \frac{dL}{L}$
- (D) The particle's kinetic energy increases by a factor of 4 when the piston is moved inward from  $L_0$  to  $\frac{1}{2}L_0$

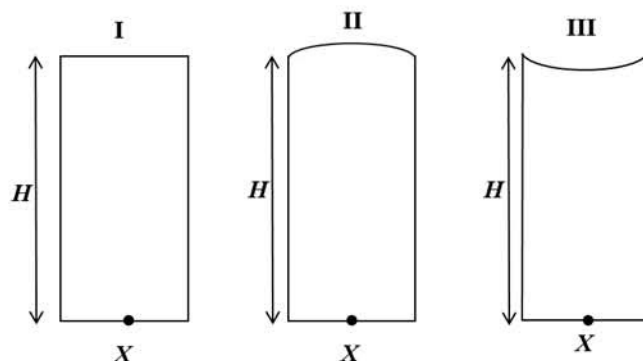
- Q.4 An electric dipole with dipole moment  $\frac{p_0}{\sqrt{2}}(\hat{i} + \hat{j})$  is held fixed at the origin O in the presence of an uniform electric field of magnitude  $E_0$ . If the potential is constant on a circle of radius  $R$  centered at the origin as shown in figure, then the correct statement(s) is/are: ( $\epsilon_0$  is permittivity of free space.  $R \gg$  dipole size)



- (A)  $R = \left( \frac{p_0}{4\pi\epsilon_0 E_0} \right)^{1/3}$
- (B) Total electric field at point A is  $\vec{E}_A = \sqrt{2}E_0(\hat{i} + \hat{j})$
- (C) Total electric field at point B is  $\vec{E}_B = 0$
- (D) The magnitude of total electric field on any two points of the circle will be same.
- Q.5 A mixture of ideal gas containing 5 moles of monatomic gas and 1 mole of rigid diatomic gas is initially at pressure  $P_0$ , volume  $V_0$ , and temperature  $T_0$ . If the gas mixture is adiabatically compressed to a volume  $V_0/4$ , then the correct statement(s) is/are, (Given  $2^{1.2} = 2.3$ ,  $2^{3.2} = 9.2$ ,  $R$  is gas constant)
- (A) The work  $|W|$  done during the process is  $13RT_0$
- (B) The average kinetic energy of the gas mixture after compression is in between  $18RT_0$  and  $19RT_0$
- (C) The final pressure of the gas mixture after compression is in between  $9P_0$  and  $10P_0$
- (D) Adiabatic constant of the gas mixture is 1.6

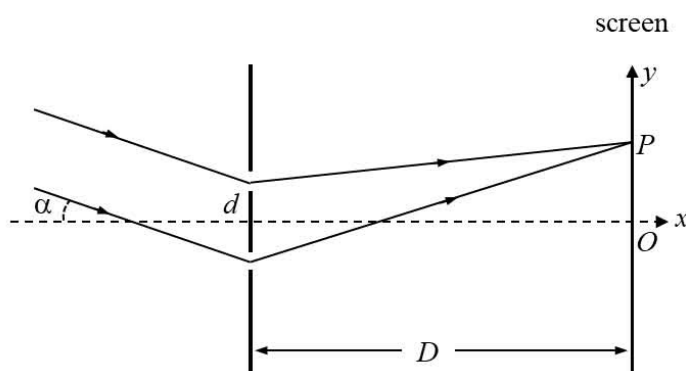


- Q.6 Three glass cylinders of equal height  $H = 30$  cm and same refractive index  $n = 1.5$  are placed on a horizontal surface as shown in figure. Cylinder I has a flat top, cylinder II has a convex top and cylinder III has a concave top. The radii of curvature of the two curved tops are same ( $R = 3$  m). If  $H_1$ ,  $H_2$ , and  $H_3$  are the apparent depths of a point  $X$  on the bottom of the three cylinders, respectively, the correct statement(s) is/are:



- (A)  $H_2 > H_1$   
 (B)  $H_3 > H_1$   
 (C)  $H_2 > H_3$   
 (D)  $0.8 \text{ cm} < (H_2 - H_1) < 0.9 \text{ cm}$

- Q.7 In a Young's double slit experiment, the slit separation  $d$  is 0.3 mm and the screen distance  $D$  is 1 m. A parallel beam of light of wavelength 600 nm is incident on the slits at angle  $\alpha$  as shown in figure. On the screen, the point  $O$  is equidistant from the slits and distance  $PO$  is 11.0 mm. Which of the following statement(s) is/are correct?



- (A) For  $\alpha = \frac{0.36}{\pi}$  degree, there will be destructive interference at point  $O$ .
- (B) For  $\alpha = 0$ , there will be constructive interference at point  $P$ .
- (C) For  $\alpha = \frac{0.36}{\pi}$  degree, there will be destructive interference at point  $P$ .
- (D) Fringe spacing depends on  $\alpha$ .
- Q.8 A free hydrogen atom after absorbing a photon of wavelength  $\lambda_a$  gets excited from the state  $n = 1$  to the state  $n = 4$ . Immediately after that the electron jumps to  $n = m$  state by emitting a photon of wavelength  $\lambda_e$ . Let the change in momentum of atom due to the absorption and the emission are  $\Delta p_a$  and  $\Delta p_e$ , respectively. If  $\lambda_a/\lambda_e = \frac{1}{5}$ , which of the option(s) is/are correct?  
[Use  $hc = 1247 \text{ eV nm}$ ;  $1 \text{ nm} = 10^{-9} \text{ m}$ ,  $h$  and  $c$  are Planck's constant and speed of light, respectively]
- (A)  $m = 2$
- (B)  $\lambda_e = 418 \text{ nm}$
- (C)  $\Delta p_a/\Delta p_e = \frac{1}{2}$
- (D) The ratio of kinetic energy of the electron in the state  $n = m$  to the state  $n = 1$  is  $\frac{1}{4}$

## SECTION 2 (Maximum Marks: 18)

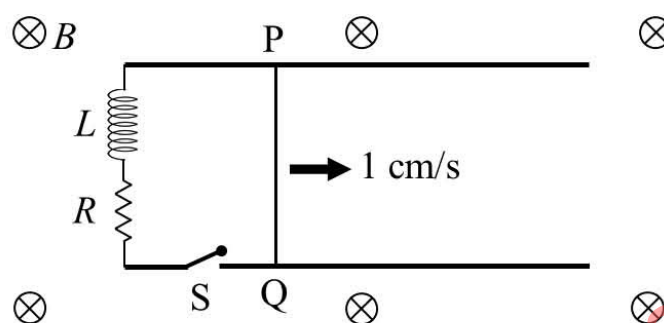
- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks* : +3 If ONLY the correct numerical value is entered;  
*Zero Marks* : 0 In all other cases.

- Q.9 A ball is thrown from ground at an angle  $\theta$  with horizontal and with an initial speed  $u_0$ . For the resulting projectile motion, the magnitude of average velocity of the ball up to the point when it hits the ground for the first time is  $V_1$ . After hitting the ground, the ball rebounds at the same angle  $\theta$  but with a reduced speed of  $u_0/\alpha$ . Its motion continues for a long time as shown in figure. If the magnitude of average velocity of the ball for entire duration of motion is  $0.8 V_1$ , the value of  $\alpha$  is \_\_\_\_\_.

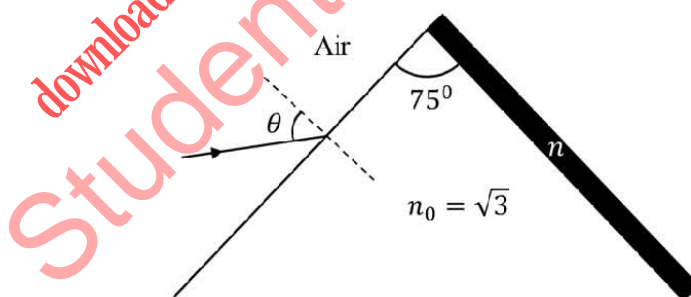


- Q.10 A 10 cm long perfectly conducting wire PQ is moving with a velocity 1 cm/s on a pair of horizontal rails of zero resistance. One side of the rails is connected to an inductor  $L = 1$  mH and a resistance  $R = 1 \Omega$  as shown in figure. The horizontal rails,  $L$  and  $R$  lie in the same plane with a uniform magnetic field  $B = 1$  T perpendicular to the plane. If the key  $S$  is closed at certain instant, the current in the circuit after 1 millisecond is  $x \times 10^{-3}$  A, where the value of  $x$  is \_\_\_\_\_.

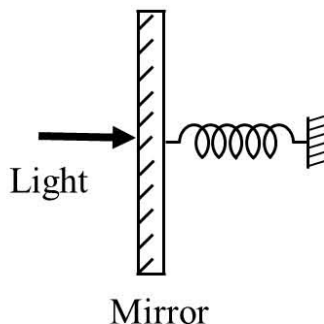
[Assume the velocity of wire PQ remains constant (1 cm/s) after key  $S$  is closed. Given:  $e^{-1} = 0.37$ , where  $e$  is base of the natural logarithm]



- Q.11 A monochromatic light is incident from air on a refracting surface of a prism of angle  $75^\circ$  and refractive index  $n_0 = \sqrt{3}$ . The other refracting surface of the prism is coated by a thin film of material of refractive index  $n$  as shown in figure. The light suffers total internal reflection at the coated prism surface for an incidence angle of  $\theta \leq 60^\circ$ . The value of  $n^2$  is \_\_\_\_\_.



- Q.12 A perfectly reflecting mirror of mass  $M$  mounted on a spring constitutes a spring-mass system of angular frequency  $\Omega$  such that  $\frac{4\pi M\Omega}{h} = 10^{24} \text{ m}^{-2}$  with  $h$  as Planck's constant.  $N$  photons of wavelength  $\lambda = 8\pi \times 10^{-6} \text{ m}$  strike the mirror simultaneously at normal incidence such that the mirror gets displaced by  $1 \mu\text{m}$ . If the value of  $N$  is  $x \times 10^{12}$ , then the value of  $x$  is \_\_\_\_\_.  
[Consider the spring as massless]



- Q.13 Suppose a  ${}^{226}_{88}\text{Ra}$  nucleus at rest and in ground state undergoes  $\alpha$ -decay to a  ${}^{222}_{86}\text{Rn}$  nucleus in its excited state. The kinetic energy of the emitted  $\alpha$  particle is found to be 4.44 MeV.  ${}^{222}_{86}\text{Rn}$  nucleus then goes to its ground state by  $\gamma$ -decay. The energy of the emitted  $\gamma$  photon is \_\_\_\_ keV.  
[Given: atomic mass of  ${}^{226}_{88}\text{Ra} = 226.005 \text{ u}$ , atomic mass of  ${}^{222}_{86}\text{Rn} = 222.000 \text{ u}$ , atomic mass of  $\alpha$  particle = 4.000 u,  $1 \text{ u} = 931 \text{ MeV}/c^2$ ,  $c$  is speed of the light]

- Q.14 An optical bench has 1.5 m long scale having four equal divisions in each cm. While measuring the focal length of a convex lens, the lens is kept at 75 cm mark of the scale and the object pin is kept at 45 cm mark. The image of the object pin on the other side of the lens overlaps with image pin that is kept at 135 cm mark. In this experiment, the percentage error in the measurement of the focal length of the lens is \_\_\_\_\_.



**SECTION 3 (Maximum Marks: 12)**

- This section contains **TWO (02)** List-Match sets.
- Each List-Match set has **TWO (02)** Multiple Choice Questions.
- Each List-Match set has two lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (I), (II), (III) and (IV) and **List-II** has **Six** entries (P), (Q), (R), (S), (T) and (U).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks* : +3 If **ONLY** the option corresponding to the correct combination is chosen;  
*Zero Marks* : 0 If none of the options is chosen (i.e., the question is unanswered);  
*Negative Marks* : -1 In all other cases.

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**Answer Q.15 and Q.16 by appropriately matching the lists based on the information given in the paragraph**

A musical instrument is made using four different metal strings, 1, 2, 3 and 4 with mass per unit length  $\mu$ ,  $2\mu$ ,  $3\mu$  and  $4\mu$  respectively. The instrument is played by vibrating the strings by varying the free length in between the range  $L_0$  and  $2L_0$ . It is found that in string-1 ( $\mu$ ) at free length  $L_0$  and tension  $T_0$  the fundamental mode frequency is  $f_0$ .

List-I gives the above four strings while list-II lists the magnitude of some quantity.

**List-I****(I)** String-1 ( $\mu$ )**(II)** String-2 ( $2\mu$ )**(III)** String-3 ( $3\mu$ )**(IV)** String-4 ( $4\mu$ )**List-II****(P)** 1**(Q)**  $1/2$ **(R)**  $1/\sqrt{2}$ **(S)**  $1/\sqrt{3}$ **(T)**  $3/16$ **(U)**  $1/16$ 

**Q.15** If the tension in each string is  $T_0$ , the correct match for the highest fundamental frequency in  $f_0$  units will be,

**(A)** I  $\rightarrow$  P, II  $\rightarrow$  Q, III  $\rightarrow$  T, IV  $\rightarrow$  S**(B)** I  $\rightarrow$  P, II  $\rightarrow$  R, III  $\rightarrow$  S, IV  $\rightarrow$  Q**(C)** I  $\rightarrow$  Q, II  $\rightarrow$  S, III  $\rightarrow$  R, IV  $\rightarrow$  P**(D)** I  $\rightarrow$  Q, II  $\rightarrow$  P, III  $\rightarrow$  R, IV  $\rightarrow$  T

**Q.16** The length of the strings 1, 2, 3 and 4 are kept fixed at  $L_0$ ,  $\frac{3L_0}{2}$ ,  $\frac{5L_0}{4}$ , and  $\frac{7L_0}{4}$ , respectively. Strings 1, 2, 3, and 4 are vibrated at their  $1^{st}$ ,  $3^{rd}$ ,  $5^{th}$ , and  $14^{th}$  harmonics, respectively such that all the strings have same frequency. The correct match for the tension in the four strings in the units of  $T_0$  will be,

**(A)** I  $\rightarrow$  P, II  $\rightarrow$  R, III  $\rightarrow$  T, IV  $\rightarrow$  U**(B)** I  $\rightarrow$  P, II  $\rightarrow$  Q, III  $\rightarrow$  T, IV  $\rightarrow$  U**(C)** I  $\rightarrow$  P, II  $\rightarrow$  Q, III  $\rightarrow$  R, IV  $\rightarrow$  T**(D)** I  $\rightarrow$  T, II  $\rightarrow$  Q, III  $\rightarrow$  R, IV  $\rightarrow$  U

**Answer Q.17 and Q.18 by appropriately matching the lists based on the information given in the paragraph**

In a thermodynamic process on an ideal monatomic gas, the infinitesimal heat absorbed by the gas is given by  $T\Delta X$ , where  $T$  is temperature of the system and  $\Delta X$  is the infinitesimal change in a thermodynamic quantity  $X$  of the system. For a mole of monatomic ideal gas  $X = \frac{3}{2}R \ln\left(\frac{T}{T_A}\right) + R \ln\left(\frac{V}{V_A}\right)$ . Here,  $R$  is gas constant,  $V$  is volume of gas,  $T_A$  and  $V_A$  are constants.

The List-I below gives some quantities involved in a process and List-II gives some possible values of these quantities.

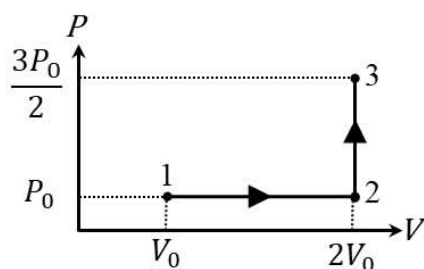
**List-I**

- (I) Work done by the system in process  $1 \rightarrow 2 \rightarrow 3$
- (II) Change in internal energy in process  $1 \rightarrow 2 \rightarrow 3$
- (III) Heat absorbed by the system in process  $1 \rightarrow 2 \rightarrow 3$
- (IV) Heat absorbed by the system in process  $1 \rightarrow 2$

**List-II**

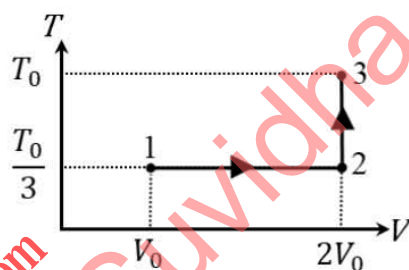
- (P)  $\frac{1}{3}RT_0 \ln 2$
- (Q)  $\frac{1}{3}RT_0$
- (R)  $RT_0$
- (S)  $\frac{4}{3}RT_0$
- (T)  $\frac{1}{3}RT_0(3 + \ln 2)$
- (U)  $\frac{5}{6}RT_0$

- Q.17 If the process carried out on one mole of monatomic ideal gas is as shown in figure in the  $PV$ -diagram with  $P_0V_0 = \frac{1}{3}RT_0$ , the correct match is,



- (A) I  $\rightarrow$  Q, II  $\rightarrow$  R, III  $\rightarrow$  P, IV  $\rightarrow$  U  
 (B) I  $\rightarrow$  Q, II  $\rightarrow$  R, III  $\rightarrow$  S, IV  $\rightarrow$  U  
 (C) I  $\rightarrow$  S, II  $\rightarrow$  R, III  $\rightarrow$  Q, IV  $\rightarrow$  T  
 (D) I  $\rightarrow$  Q, II  $\rightarrow$  S, III  $\rightarrow$  R, IV  $\rightarrow$  U

- Q.18 If the process on one mole of monatomic ideal gas is as shown in the  $TV$ -diagram with  $P_0V_0 = \frac{1}{3}RT_0$ , the correct match is,



- (A) I  $\rightarrow$  P, II  $\rightarrow$  R, III  $\rightarrow$  T, IV  $\rightarrow$  S  
 (B) I  $\rightarrow$  P, II  $\rightarrow$  T, III  $\rightarrow$  Q, IV  $\rightarrow$  T  
 (C) I  $\rightarrow$  P, II  $\rightarrow$  R, III  $\rightarrow$  T, IV  $\rightarrow$  P  
 (D) I  $\rightarrow$  S, II  $\rightarrow$  T, III  $\rightarrow$  Q, IV  $\rightarrow$  U

**JEE (ADVANCED) 2019 PAPER 2**  
**PART-II CHEMISTRY**

**SECTION 1 (Maximum Marks: 32)**

- This section contains **EIGHT (08)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:  
Full Marks : +4 If only (all) the correct option(s) is(are) chosen;  
Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;  
Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen and both of which are correct;  
Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;  
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
Negative Marks : -1 In all other cases.
- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then  
choosing **ONLY** (A), (B) and (D) will get +4 marks;  
choosing **ONLY** (A) and (B) will get +2 marks;  
choosing **ONLY** (A) and (D) will get +2 marks;  
choosing **ONLY** (B) and (D) will get +2 marks;  
choosing **ONLY** (A) will get +1 mark;  
choosing **ONLY** (B) will get +1 mark;  
choosing **ONLY** (D) will get +1 mark;  
choosing no option (i.e. the question is unanswered) will get 0 marks; and  
choosing any other combination of options will get -1 mark.

- Q.1 The cyanide process of gold extraction involves leaching out gold from its ore with  $\text{CN}^-$  in the presence of Q in water to form R. Subsequently, R is treated with T to obtain Au and Z. Choose the correct option(s)
- (A) Q is  $\text{O}_2$
- (B) T is Zn
- (C) Z is  $[\text{Zn}(\text{CN})_4]^{2-}$
- (D) R is  $[\text{Au}(\text{CN})_4]^-$
- Q.2 With reference to *aqua regia*, choose the correct option(s)
- (A) *Aqua regia* is prepared by mixing conc. HCl and conc.  $\text{HNO}_3$  in 3:1 (v/v) ratio
- (B) Reaction of gold with *aqua regia* produces an anion having Au in +3 oxidation state
- (C) Reaction of gold with *aqua regia* produces  $\text{NO}_2$  in the absence of air
- (D) The yellow colour of *aqua regia* is due to the presence of  $\text{NOCl}$  and  $\text{Cl}_2$



Q.3 Consider the following reactions (unbalanced)



Choose the correct option(s)

- (A) Z is dirty white in colour
- (B) The oxidation state of Zn in T is +1
- (C) R is a V-shaped molecule
- (D) Bond order of Q is 1 in its ground state

Q.4 The ground state energy of hydrogen atom is  $-13.6 \text{ eV}$ . Consider an electronic state  $\Psi$  of  $\text{He}^+$  whose energy, azimuthal quantum number and magnetic quantum number are  $-3.4 \text{ eV}$ , 2 and 0, respectively. Which of the following statement(s) is(are) true for the state  $\Psi$ ?

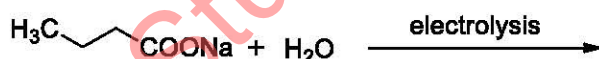
- (A) It is a  $4d$  state
- (B) It has 2 angular nodes
- (C) It has 3 radial nodes
- (D) The nuclear charge experienced by the electron in this state is less than  $2e$ , where  $e$  is the magnitude of the electronic charge

Q.5 Which of the following reaction(s) produce(s) propane as a major product?

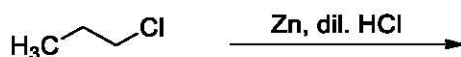
(A)



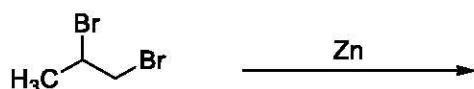
(B)



(C)

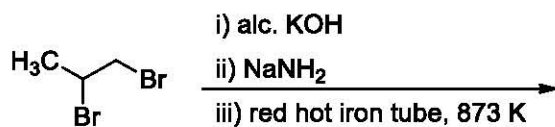


(D)

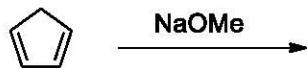


Q.6 Choose the correct option(s) that give(s) an aromatic compound as the major product

(A)



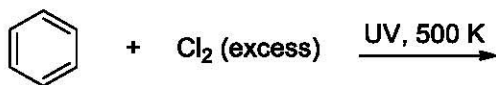
(B)



(C)

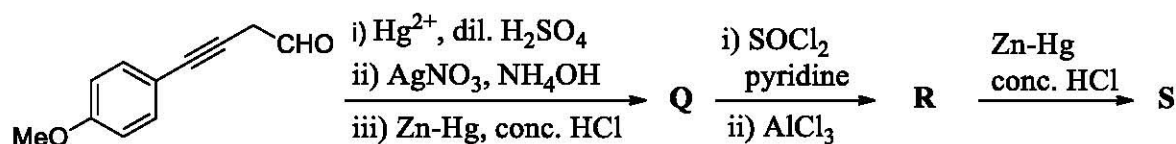


(D)



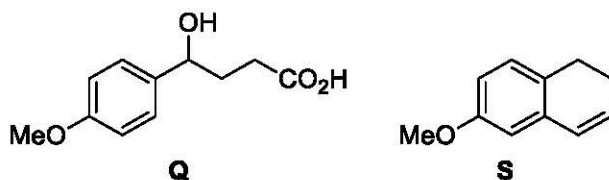
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Q.7 Choose the correct option(s) for the following reaction sequence

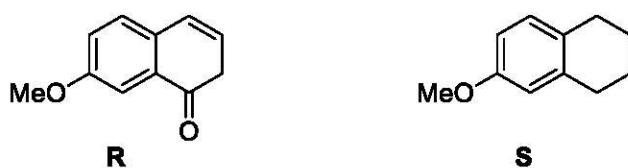


Consider Q, R and S as major products

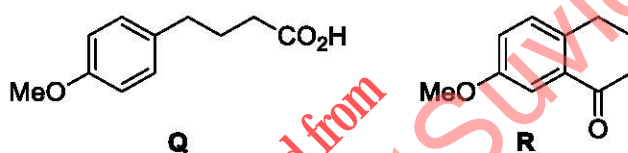
(A)



(B)



(C)



(D)



Q.8 Choose the correct option(s) from the following

(A) Natural rubber is polyisoprene containing *trans* alkene units

(B) Nylon-6 has amide linkages

(C) Teflon is prepared by heating tetrafluoroethene in presence of a persulphate catalyst at high pressure

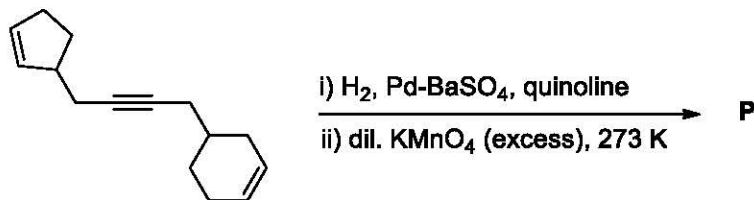
(D) Cellulose has only  $\alpha$ -D-glucose units that are joined by glycosidic linkages

**SECTION 2 (Maximum Marks: 18)**

- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks* : +3 If **ONLY** the correct numerical value is entered;  
*Zero Marks* : 0 In all other cases.

- Q.9 The amount of water produced (in g) in the oxidation of 1 mole of rhombic sulphur by conc.  $\text{HNO}_3$  to a compound with the highest oxidation state of sulphur is \_\_\_\_\_.  
(Given data: Molar mass of water =  $18 \text{ g mol}^{-1}$ )
- Q.10 Total number of *cis* N–Mn–Cl bond angles (that is, Mn–N and Mn–Cl bonds in *cis* positions) present in a molecule of *cis*- $[\text{Mn}(\text{en})_2\text{Cl}_2]$  complex is \_\_\_\_\_. (*en* =  $\text{NH}_2\text{CH}_2\text{CH}_2\text{NH}_2$ )
- Q.11 The decomposition reaction,  $2\text{N}_2\text{O}_5(\text{g}) \xrightarrow{\Delta} 2\text{N}_2\text{O}_4(\text{g}) + \text{O}_2(\text{g})$  is started in a closed cylinder under isothermal isochoric condition at an initial pressure of 1 atm. After  $Y \times 10^3 \text{ s}$ , the pressure inside the cylinder is found to be 1.45 atm. If the rate constant of the reaction is  $5 \times 10^{-4} \text{ s}^{-1}$ , assuming ideal gas behavior, the value of Y is \_\_\_\_\_
- Q.12 The mole fraction of urea in an aqueous urea solution containing 900 g of water is 0.05. If the density of the solution is  $1.2 \text{ g cm}^{-3}$ , the molarity of urea solution is \_\_\_\_\_.  
(Given data: Molar masses of urea and water are  $60 \text{ g mol}^{-1}$  and  $18 \text{ g mol}^{-1}$ , respectively)

Q.13 Total number of hydroxyl groups present in a molecule of the major product P is \_\_\_\_



Q.14 Total number of isomers, considering both structural and stereoisomers, of cyclic ethers with the molecular formula C<sub>4</sub>H<sub>8</sub>O is \_\_\_\_

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**SECTION 3 (Maximum Marks: 12)**

- This section contains **TWO (02)** List-Match sets.
- Each List-Match set has **TWO (02)** Multiple Choice Questions.
- Each List-Match set has two lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (I), (II), (III) and (IV) and **List-II** has **Six** entries (P), (Q), (R), (S), (T) and (U).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:  
Full Marks : +3 If **ONLY** the option corresponding to the correct combination is chosen;  
Zero Marks : 0 If none of the options is chosen (i.e., the question is unanswered);  
Negative Marks : -1 In all other cases.

Answer Q.15 and Q.16 by appropriately matching the lists based on the information given in the paragraph

Consider the Bohr's model of a one-electron atom where the electron moves around the nucleus. In the following, List-I contains some quantities for the  $n^{\text{th}}$  orbit of the atom and List-II contains options showing how they depend on  $n$ .

**List-I**

- (I) Radius of the  $n^{\text{th}}$  orbit
- (II) Angular momentum of the electron in the  $n^{\text{th}}$  orbit
- (III) Kinetic energy of the electron in the  $n^{\text{th}}$  orbit
- (IV) Potential energy of the electron in the  $n^{\text{th}}$  orbit

**List-II**

- (P)  $\propto n^{-2}$
- (Q)  $\propto n^{-1}$
- (R)  $\propto n^0$
- (S)  $\propto n^1$
- (T)  $\propto n^2$
- (U)  $\propto n^{1/2}$

Q.15 Which of the following options has the correct combination considering List-I and List-II?

- (A) (I), (P)      (B) (I), (T)      (C) (II), (Q)      (D) (II), (R)

Q.16 Which of the following options has the correct combination considering List-I and List-II?

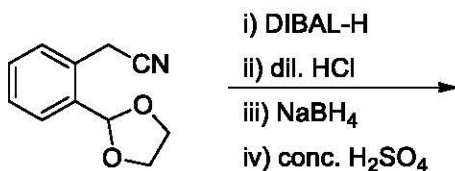
- (A) (III), (P)      (B) (III), (S)      (C) (IV), (Q)      (D) (IV), (U)

Answer Q.17 and Q.18 by appropriately matching the lists based on the information given in the paragraph

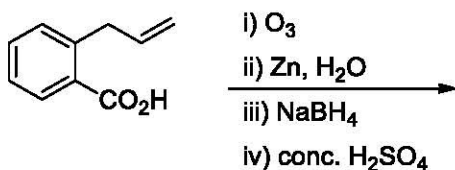
List-I includes starting materials and reagents of selected chemical reactions. List-II gives structures of compounds that may be formed as intermediate products and/or final products from the reactions of List-I.

## List-I

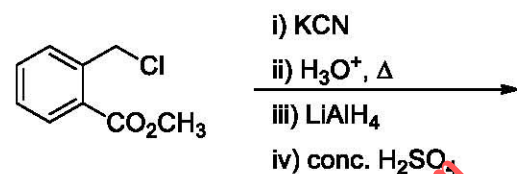
(I)



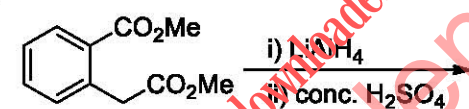
(II)



(III)

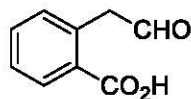


(IV)

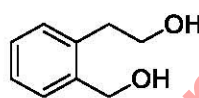


## List-II

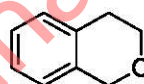
(P)



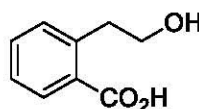
(Q)



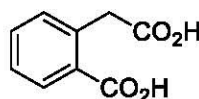
(R)



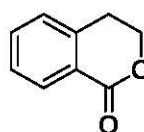
(S)



(T)



(U)



Q.17 Which of the following options has correct combination considering List-I and List-II?

- |                         |                         |
|-------------------------|-------------------------|
| (A) (I), (Q), (T), (U)  | (B) (II), (P), (S), (T) |
| (C) (II), (P), (S), (U) | (D) (I), (S), (Q), (R)  |

Q.18 Which of the following options has correct combination considering List-I and List-II?

- |                     |                    |
|---------------------|--------------------|
| (A) (III), (S), (R) | (B) (IV), (Q), (U) |
| (C) (III), (T), (U) | (D) (IV), (Q), (R) |

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## JEE (ADVANCED) 2019 PAPER 2

### PART-III MATHEMATICS

#### SECTION 1 (Maximum Marks: 32)

- This section contains **EIGHT (08)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +4 If only (all) the correct option(s) is(are) chosen;  
 Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;  
 Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen and both of which are correct;  
 Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.
- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then  
 choosing **ONLY** (A), (B) and (D) will get +4 marks;  
 choosing **ONLY** (A) and (B) will get +2 marks;  
 choosing **ONLY** (A) and (D) will get +2 marks;  
 choosing **ONLY** (B) and (D) will get +2 marks;  
 choosing **ONLY** (A) will get +1 mark;  
 choosing **ONLY** (B) will get +1 mark;  
 choosing **ONLY** (D) will get +1 mark;  
 choosing no option (i.e. the question is unanswered) will get 0 marks; and  
 choosing any other combination of options will get -1 mark.

Q.1 Let

$$P_1 = I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad P_2 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, \quad P_3 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix},$$

$$P_4 = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}, \quad P_5 = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}, \quad P_6 = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$\text{and } X = \sum_{k=1}^6 P_k \begin{bmatrix} 2 & 1 & 3 \\ 1 & 0 & 2 \\ 3 & 2 & 1 \end{bmatrix} P_k^T$$

where  $P_k^T$  denotes the transpose of the matrix  $P_k$ . Then which of the following options is/are correct?

- (A) If  $X \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \alpha \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ , then  $\alpha = 30$
- (B)  $X$  is a symmetric matrix
- (C) The sum of diagonal entries of  $X$  is 18
- (D)  $X - 30I$  is an invertible matrix

Q.2 Let  $x \in \mathbb{R}$  and let

$$P = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 2 & 2 \\ 0 & 0 & 3 \end{bmatrix}, \quad Q = \begin{bmatrix} 2 & x & x \\ 0 & 4 & 0 \\ x & x & 6 \end{bmatrix} \text{ and } R = PQP^{-1}.$$

Then which of the following options is/are correct?

(A) There exists a real number  $x$  such that  $PQ = QP$

(B)  $\det R = \det \begin{bmatrix} 2 & x & x \\ 0 & 4 & 0 \\ x & x & 5 \end{bmatrix} + 8$ , for all  $x \in \mathbb{R}$

(C) For  $x = 0$ , if  $R \begin{bmatrix} 1 \\ a \\ b \end{bmatrix} = 6 \begin{bmatrix} 1 \\ a \\ b \end{bmatrix}$ , then  $a + b = 5$

(D) For  $x = 1$ , there exists a unit vector  $\alpha \hat{i} + \beta \hat{j} + \gamma \hat{k}$  for which  $R \begin{bmatrix} \alpha \\ \beta \\ \gamma \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$

Q.3 For non-negative integers  $n$ , let

$$f(n) = \frac{\sum_{k=0}^n \sin\left(\frac{k+1}{n+2}\pi\right) \sin\left(\frac{k+2}{n+2}\pi\right)}{\sum_{k=0}^n \sin^2\left(\frac{k+1}{n+2}\pi\right)}$$

Assuming  $\cos^{-1}x$  takes values in  $[0, \pi]$ , which of the following options is/are correct?

(A)  $f(4) = \frac{\sqrt{3}}{2}$

(B)  $\lim_{n \rightarrow \infty} f(n) = \frac{1}{2}$

(C) If  $\alpha = \tan(\cos^{-1}f(6))$ , then  $\alpha^2 + 2\alpha - 1 = 0$

(D)  $\sin(7 \cos^{-1}f(5)) = 0$

Q.4 Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a function. We say that  $f$  has

PROPERTY 1 if  $\lim_{h \rightarrow 0} \frac{f(h) - f(0)}{\sqrt{|h|}}$  exists and is finite, and

PROPERTY 2 if  $\lim_{h \rightarrow 0} \frac{f(h) - f(0)}{h^2}$  exists and is finite.

Then which of the following options is/are correct?

- (A)  $f(x) = |x|$  has PROPERTY 1                      (B)  $f(x) = x^{2/3}$  has PROPERTY 1  
 (C)  $f(x) = x|x|$  has PROPERTY 2                      (D)  $f(x) = \sin x$  has PROPERTY 2

Q.5 Let

$$f(x) = \frac{\sin \pi x}{x^2}, \quad x > 0.$$

Let  $x_1 < x_2 < x_3 < \dots < x_n < \dots$  be all the points of local maximum of  $f$  and  $y_1 < y_2 < y_3 < \dots < y_n < \dots$  be all the points of local minimum of  $f$ .

Then which of the following options is/are correct?

- (A)  $x_1 < y_1$                       (B)  $x_{n+1} - x_n > 2$  for every  $n$   
 (C)  $x_n \in \left(2n, 2n + \frac{1}{2}\right)$  for every  $n$                       (D)  $|x_n - y_n| > 1$  for every  $n$

Q.6 For  $a \in \mathbb{R}$ ,  $|a| > 1$ , let

$$\lim_{n \rightarrow \infty} \left( \frac{1 + \sqrt[3]{2} + \dots + \sqrt[3]{n}}{n^{7/3} \left( \frac{1}{(an+1)^2} + \frac{1}{(an+2)^2} + \dots + \frac{1}{(an+n)^2} \right)} \right) = 54.$$

Then the possible value(s) of  $a$  is/are

- (A)  $-9$                       (B)  $-6$                       (C)  $7$                       (D)  $8$



Q.7 Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be given by  $f(x) = (x-1)(x-2)(x-5)$ . Define

$$F(x) = \int_0^x f(t) dt, \quad x > 0.$$

Then which of the following options is/are correct?

- (A)  $F$  has a local minimum at  $x = 1$
- (B)  $F$  has a local maximum at  $x = 2$
- (C)  $F$  has two local maxima and one local minimum in  $(0, \infty)$
- (D)  $F(x) \neq 0$  for all  $x \in (0, 5)$

Q.8 Three lines

$$L_1: \quad \vec{r} = \lambda \hat{i}, \quad \lambda \in \mathbb{R},$$

$$L_2: \quad \vec{r} = \hat{k} + \mu \hat{j}, \quad \mu \in \mathbb{R} \text{ and}$$

$$L_3: \quad \vec{r} = \hat{i} + \hat{j} + \nu \hat{k}, \quad \nu \in \mathbb{R}$$

are given. For which point(s)  $Q$  on  $L_2$  can we find a point  $P$  on  $L_1$  and a point  $R$  on  $L_3$  so that  $P, Q$  and  $R$  are collinear?

(A)  $\hat{k} - \frac{1}{2}\hat{j}$

(B)  $\hat{k}$

(C)  $\hat{k} + \frac{1}{2}\hat{j}$

(D)  $\hat{k} + \hat{j}$

**SECTION 2 (Maximum Marks: 18)**

- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks* : +3 If **ONLY** the correct numerical value is entered;  
*Zero Marks* : 0 In all other cases.

Q.9 Suppose

$$\det \begin{bmatrix} \sum_{k=0}^n k & \sum_{k=0}^n {}^nC_k k^2 \\ \sum_{k=0}^n {}^nC_k k & \sum_{k=0}^n {}^nC_k 3^k \end{bmatrix} = 0$$

holds for some positive integer  $n$ . Then  $\sum_{k=0}^n \frac{{}^nC_k}{k+1}$  equals \_\_\_\_

Q.10 Five persons  $A, B, C, D$  and  $E$  are seated in a circular arrangement. If each of them is given a hat of one of the three colours red, blue and green, then the number of ways of distributing the hats such that the persons seated in adjacent seats get different coloured hats is \_\_\_\_

Q.11 Let  $|X|$  denote the number of elements in a set  $X$ . Let  $S = \{1, 2, 3, 4, 5, 6\}$  be a sample space, where each element is equally likely to occur. If  $A$  and  $B$  are independent events associated with  $S$ , then the number of ordered pairs  $(A, B)$  such that  $1 \leq |B| < |A|$ , equals \_\_\_\_

Q.12 The value of

$$\sec^{-1} \left( \frac{1}{4} \sum_{k=0}^{10} \sec \left( \frac{7\pi}{12} + \frac{k\pi}{2} \right) \sec \left( \frac{7\pi}{12} + \frac{(k+1)\pi}{2} \right) \right)$$

in the interval  $\left[ -\frac{\pi}{4}, \frac{3\pi}{4} \right]$  equals \_\_\_\_

Q.13 The value of the integral

$$\int_0^{\pi/2} \frac{3 \sqrt{\cos \theta}}{(\sqrt{\cos \theta} + \sqrt{\sin \theta})^5} d\theta$$

equals \_\_\_\_

Q.14 Let  $\vec{a} = 2\hat{i} + \hat{j} - \hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} + \hat{k}$  be two vectors. Consider a vector  $\vec{c} = \alpha\vec{a} + \beta\vec{b}$ ,  $\alpha, \beta \in \mathbb{R}$ . If the projection of  $\vec{c}$  on the vector  $(\vec{a} + \vec{b})$  is  $3\sqrt{2}$ , then the minimum value of  $(\vec{c} - (\vec{a} \times \vec{b})) \cdot \vec{c}$  equals \_\_\_\_

**SECTION 3 (Maximum Marks: 12)**

- This section contains **TWO (02)** List-Match sets.
- Each List-Match set has **TWO (02)** Multiple Choice Questions.
- Each List-Match set has two lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (I), (II), (III) and (IV) and **List-II** has **Six** entries (P), (Q), (R), (S), (T) and (U).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks* : +3 If **ONLY** the option corresponding to the correct combination is chosen;  
*Zero Marks* : 0 If none of the options is chosen (i.e., the question is unanswered);  
*Negative Marks* : -1 In all other cases.

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Answer Q.15 and Q.16 by appropriately matching the lists based on the information given in the paragraph.

Let  $f(x) = \sin(\pi \cos x)$  and  $g(x) = \cos(2\pi \sin x)$  be two functions defined for  $x > 0$ . Define the following sets whose elements are written in the increasing order:

$$X = \{x : f(x) = 0\}, \quad Y = \{x : f'(x) = 0\},$$

$$Z = \{x : g(x) = 0\}, \quad W = \{x : g'(x) = 0\}.$$

List – I contains the sets  $X$ ,  $Y$ ,  $Z$  and  $W$ . List – II contains some information regarding these sets.

List–I

(I)  $X$

(II)  $Y$

(III)  $Z$

(IV)  $W$

List–II

(P)  $\supseteq \left\{ \frac{\pi}{2}, \frac{3\pi}{2}, 4\pi, 7\pi \right\}$

(Q) an arithmetic progression

(R) NOT an arithmetic progression

(S)  $\supseteq \left\{ \frac{\pi}{6}, \frac{7\pi}{6}, \frac{13\pi}{6} \right\}$

(T)  $\supseteq \left\{ \frac{\pi}{3}, \frac{2\pi}{3}, \pi \right\}$

(U)  $\supseteq \left\{ \frac{\pi}{6}, \frac{3\pi}{4} \right\}$

Q.15 Which of the following is the only CORRECT combination?

(A) (I), (P), (R) (B) (II), (Q), (T) (C) (I), (Q), (U) (D) (II), (R), (S)

Q.16 Which of the following is the only CORRECT combination?

(A) (III), (R), (U) (B) (IV), (P), (R), (S)  
(C) (III), (P), (Q), (U) (D) (IV), (Q), (T)

Answer Q.17 and Q.18 by appropriately matching the lists based on the information given in the paragraph.

Let the circles  $C_1 : x^2 + y^2 = 9$  and  $C_2 : (x - 3)^2 + (y - 4)^2 = 16$ , intersect at the points  $X$  and  $Y$ . Suppose that another circle  $C_3 : (x - h)^2 + (y - k)^2 = r^2$  satisfies the following conditions:

- (i) centre of  $C_3$  is collinear with the centres of  $C_1$  and  $C_2$ ,
- (ii)  $C_1$  and  $C_2$  both lie inside  $C_3$ , and
- (iii)  $C_3$  touches  $C_1$  at  $M$  and  $C_2$  at  $N$ .

Let the line through  $X$  and  $Y$  intersect  $C_3$  at  $Z$  and  $W$ , and let a common tangent of  $C_1$  and  $C_3$  be a tangent to the parabola  $x^2 = 8ay$ .

There are some expressions given in the List-I whose values are given in List-II below:

## List-I

(I)  $2h + k$

(II)  $\frac{\text{Length of } ZW}{\text{Length of } XY}$

(III)  $\frac{\text{Area of triangle } MZN}{\text{Area of triangle } ZMW}$

(IV)  $\alpha$

## List-II

(P) 6

(Q)  $\sqrt{6}$

(R)  $\frac{5}{4}$

(S)  $\frac{21}{5}$

(T)  $2\sqrt{6}$

(U)  $\frac{10}{3}$

Q.17 Which of the following is the only CORRECT combination?

- (A) (I), (S)      (B) (I), (U)      (C) (II), (Q)      (D) (II), (T)

Q.18 Which of the following is the only INCORRECT combination?

- (A) (I), (P)      (B) (IV), (U)      (C) (III), (R)      (D) (IV), (S)